## **Homework #10 (100 points) - Show all work on the following problems:** (Grading rubric: Solid attempt = 50% credit, Correct approach but errors = 75% credit, Correct original solution = 100% credit, Copy of online solutions = 0% credit)

**Problem 1 (30 points):** An infinite thick slab lies in the x-y plane, extending from z = -a/2 to z = +a/2. The slab carries a uniform volume current *J* pointing in the +x-direction. Find the magnitude and direction of the magnetic field, as function of z, inside and outside the slab.

**Problem 2 (20 points):** Consider a large parallel-plate capacitor with uniform charge density  $\sigma$  on the top plate, and  $-\sigma$  on the bottom plate, moving with a constant speed *v* tangential to the surface of the plates.

**2a (10 point):** Find the magnetic field between the plates and above and below them.

**2b (10 point):** Find the magnitude and direction of the magnetic force per unit area on the upper plate (caused by the bottom plate).

**Problem 3 (30 points):** Consider a finite segment of wire aligned with the z-axis, extending from point  $z_1$  to  $z_2$ , and carrying a current *I*.

**3a (15 points):** Find the magnetic vector potential at a radial distance *s* from the origin.

**3b (15 points):** Show that the curl of this magnetic vector potential gives the same magnetic field as derived in Ex. 5.5.

**Problem 4 (20 points):** Find the magnetic vector potential above and below an infinite plane (in the x-y plane) with a surface current density *K* flowing in the x-direction.